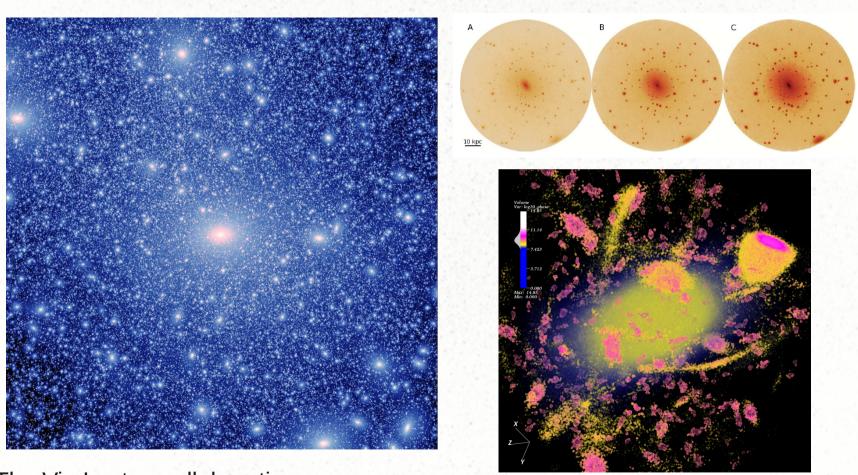
Dark Matter Clumps and Streams From Numerical Simulations to Detection Efforts

Michael Kuhlen, UC Berkeley



The Via Lactea collaboration (P. Madau, J. Diemand, M. Zemp, B. Moore, J. Stadel, D. Potter, V. Rashkov)

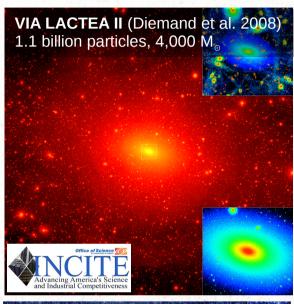
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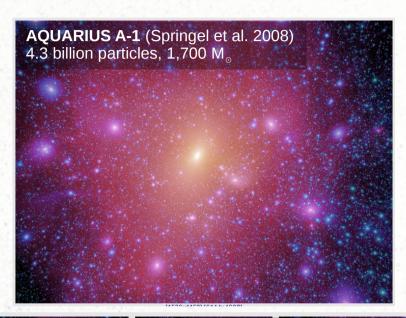
Outline

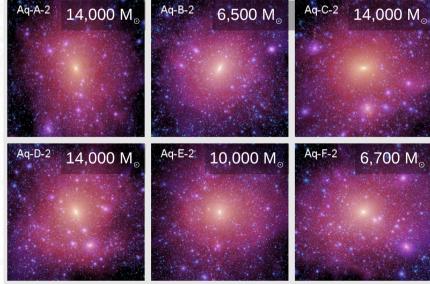
- Numerical Simulations State-of-the-Art
- Substructure: Astrophysics
- Substructure: Particle physics
 - As individual sources of DM annihilation: dwarf galaxies and dark subhalos
 - As a diffuse background from the cumulative annihilation in all Galactic subhalos
 - As an annihilation "boost factor"
 - As signatures in direct detection experiments
- Conclusions

I. Dark Matter Simulations: The State Of The Art

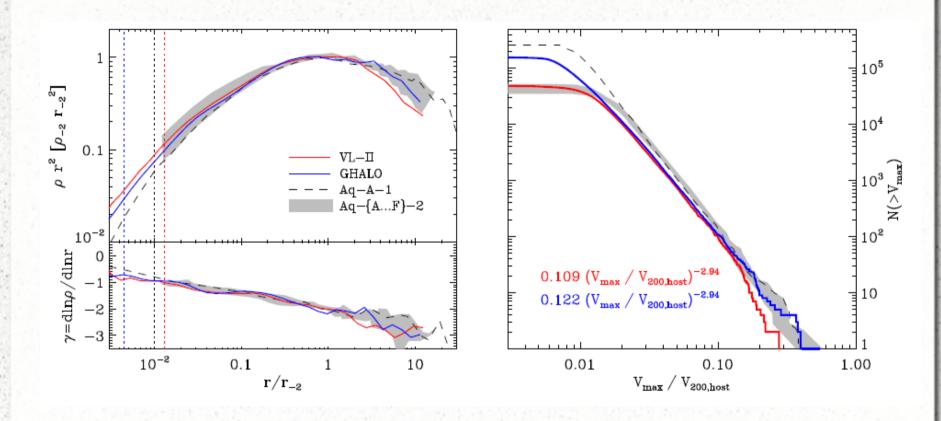








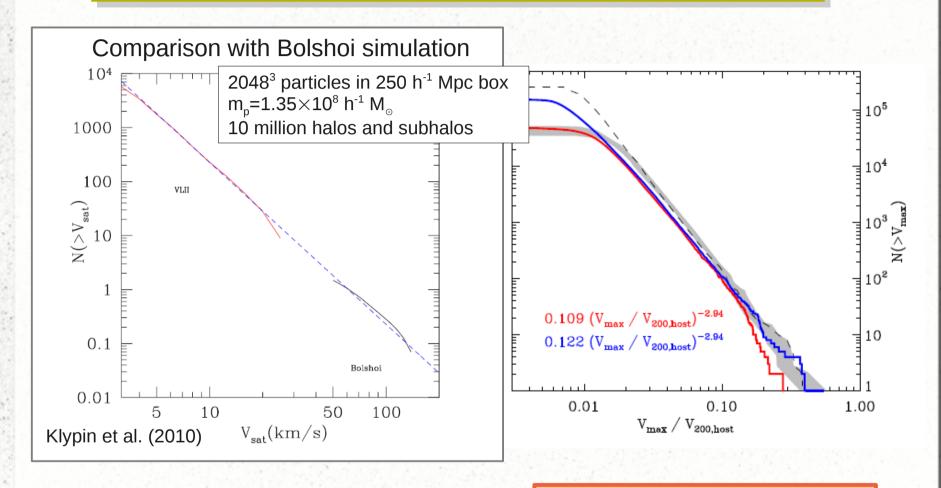
Via Lactea II/GHALO vs. Aquarius



Via Lactea II, GHALO: **PKDGRAV2m** Aquarius: **Gadget-3**

Once appropriately scaled, VL-II, GHALO, and Aquarius agree with each other.

Via Lactea II/GHALO vs. Aquarius

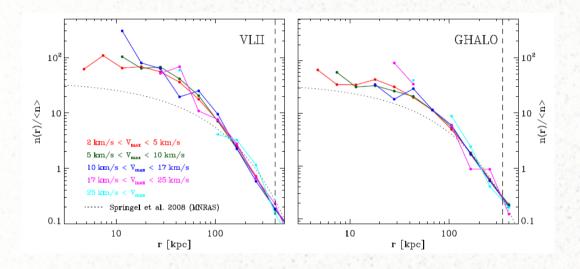


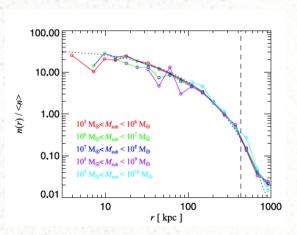
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Once appropriately scaled, VL-II, GHALO, and Aquarius agree with each other.

Via Lactea II/GHALO vs. Aquarius

Some differences remain, e.g. in the radial distribution of subhalos.

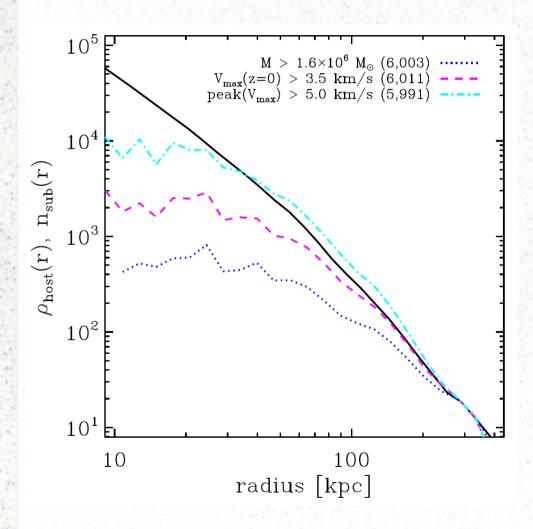




Possible explanations:

- > Slightly different cosmology? σ_8 =0.76, n_s=0.96 in VL2/GHALO σ_8 =0.9, n_s=1 in Aquarius
- > Different subhalo finders? 6DFOF vs. SUBFIND
- Different sample selection? V_{max} vs. M

The Radial Distribution of Subhalos Depends on Selection



The subhalo radial distribution is **anti-biased** with respect to the DM density: fewer subhalos in the center.

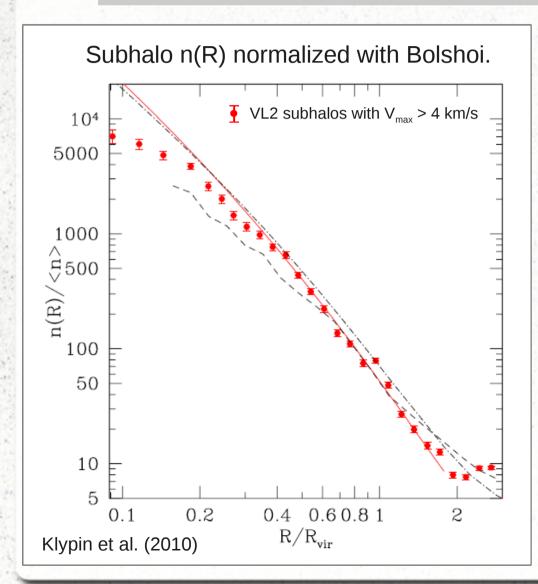
(cf. Ghigna et al. 2000; de Lucia et al. 2004)

Depends on how one selection:

- strongest for M(z=0)-selected,
- weaker for Vmax(z=0)-selected,
- disappears down to ~30 kpc for peak(Vmax)-selected.

(cf. Nagai & Kravtsov 2005; Faltenbacher & Diemand 2006)

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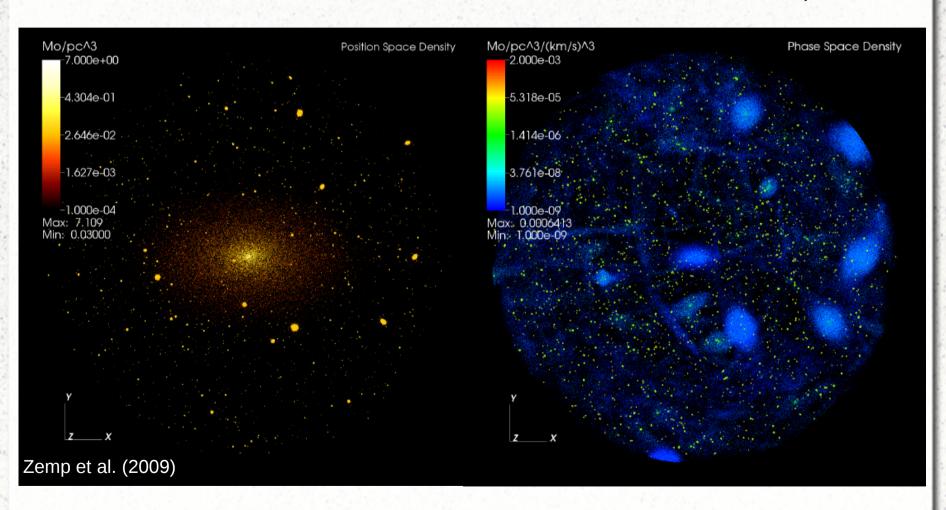
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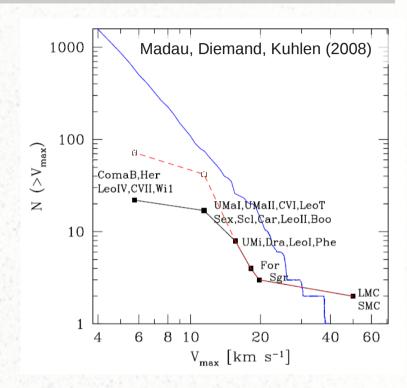
Velocity Space Substructure

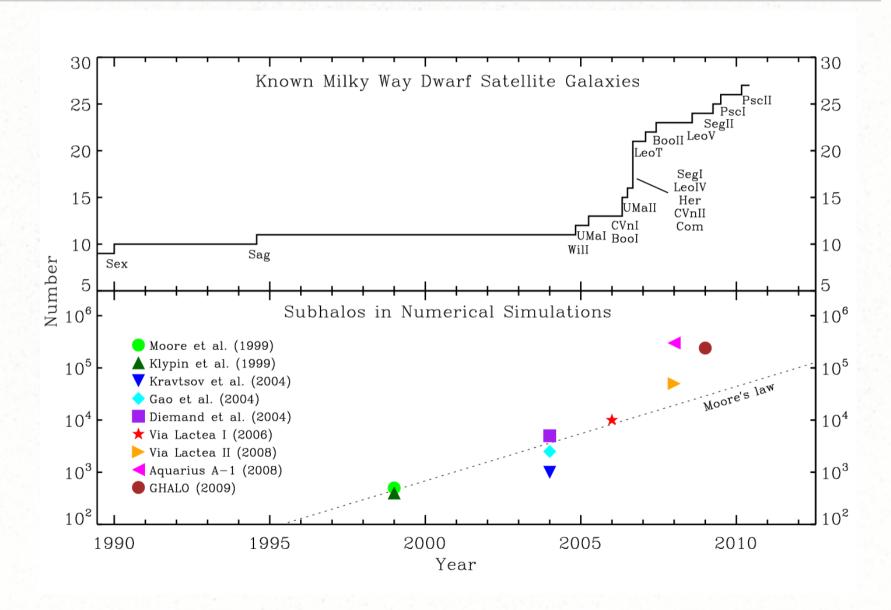
Whereas previous simulations were almost completely smooth in the central region, with VL-II we resolve lots of subhalos and tidal streams even down to 8 kpc.



Hosts for Dwarf Galaxies

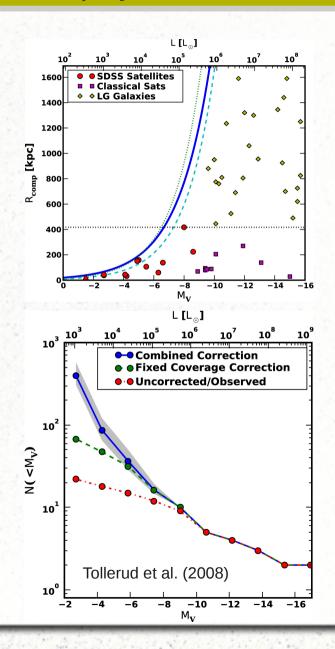
- The Missing Satellites Problem
- How well do stellar radial velocities constrain the halo mass and the central phase space density?
- What does this tell us about the nature of DM?
- Galactic disk bombardment
 - Heating, warps
 - Non-axisymmetric spiral structure in HI?
- > Effect on cold stellar tidal streams
 - gaps, kinks?
- > Effect on strong gravitational lensing:
 - Flux ratio anomalies
 - Time delay perturbations





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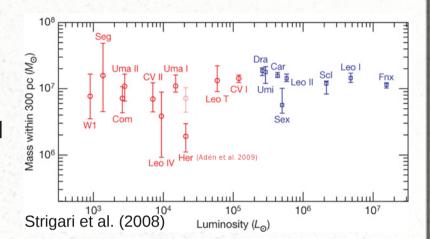


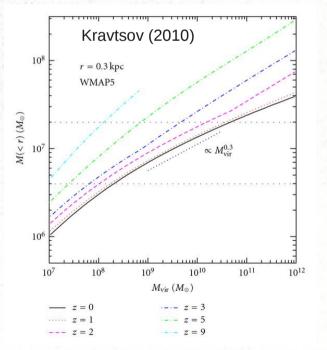
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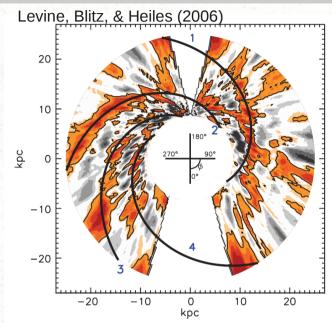


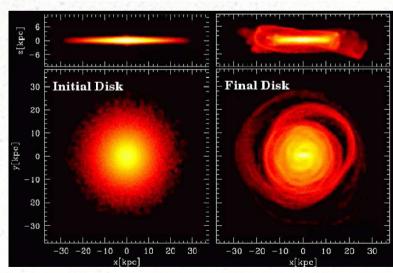
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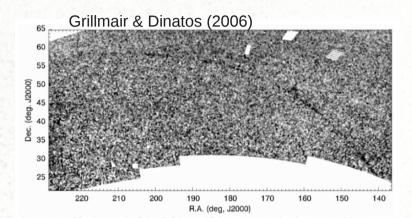
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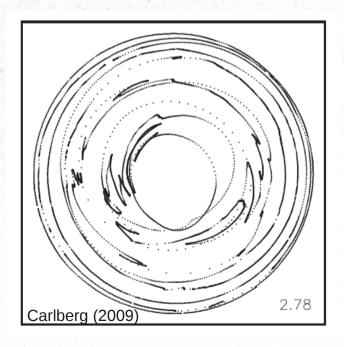




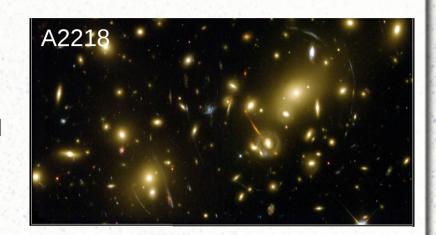
Kazantzidis et al. (2010)

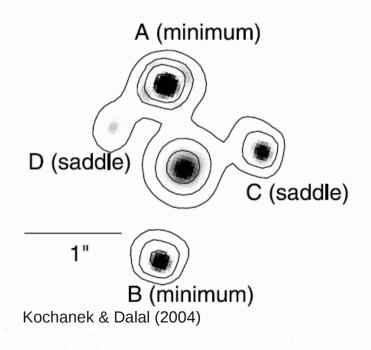
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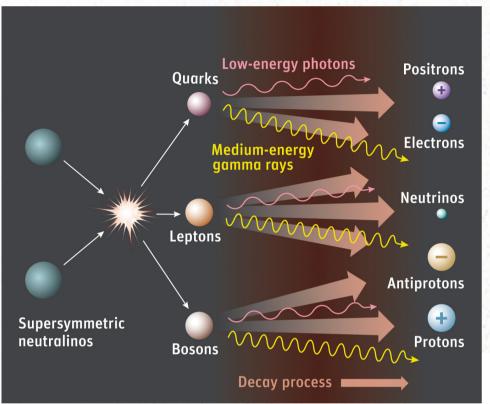




Dark Matter Substructure: Particle Physics

- 1) Subhalos as individual DM annihilation sources
 - a) Luminous dwarf satellite galaxies
 - b) Dark subhalos
- 2) Cumulative signal from all Galactic subhalos
- 3) Substructure "boost factor"
- 4) Velocity substructure and Direct Detection

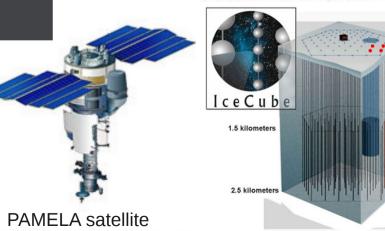
DM annihilation and its signals



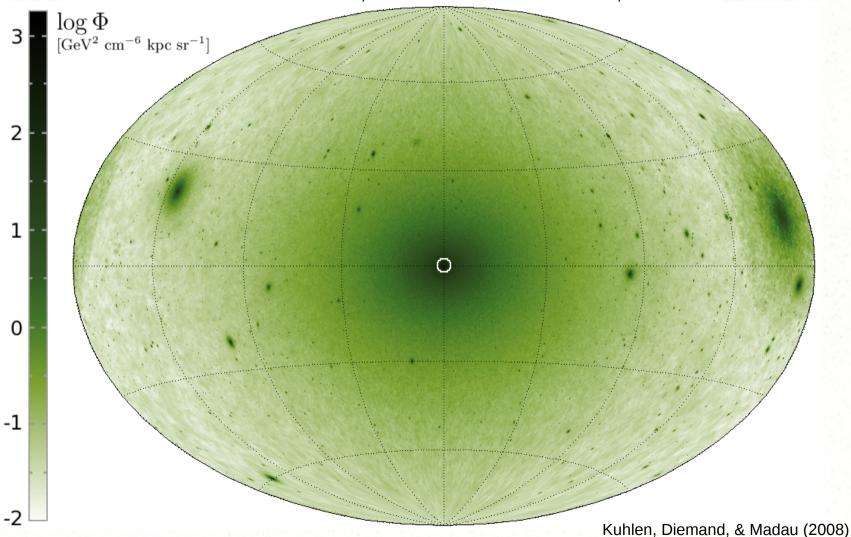








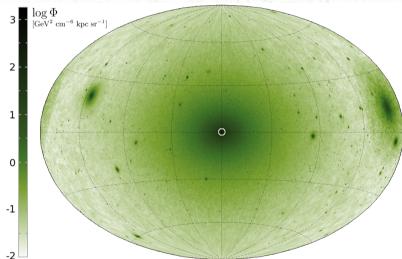
$$N_{\gamma} = \left[\int_{\text{line of sight}}^{\rho_{\text{DM}}} dl(\psi) \right] \frac{\langle \sigma v \rangle}{2M_{\chi}^{2}} \left[\int_{E_{th}}^{M_{\chi}} \left(\frac{dN_{\gamma}}{dE} \right) A_{\text{eff}}(E) dE \right] \frac{\Delta \Omega}{4\pi} \tau_{\text{exp}}$$



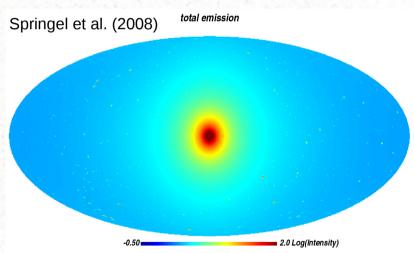
$$N_{\gamma} = \left[\int_{\text{line of sight}}^{2} dl(\psi) \right] \frac{\langle \sigma v \rangle}{2M_{\chi}^{2}} \left[\int_{E_{th}}^{M_{\chi}} \left(\frac{dN_{\gamma}}{dE} \right) A_{\text{eff}}(E) dE \right] \frac{\Delta \Omega}{4\pi} \tau_{\text{exp}}$$

Huh? How come these look so different?





Kuhlen, Diemand, & Madau (2008)



Aquarius

For simplicity and for better visual representation they [the subhalos] have been represented as point sources that were smoothed with a Gaussian beam of 40 arcmin.

Fermi/LAT GTOBSSIM Monte-Carlo Simulation (with Brandon Anderson & Robert Johnson, SCIPP)

LAT A_{eff} dependence on viewing angle and photon energy

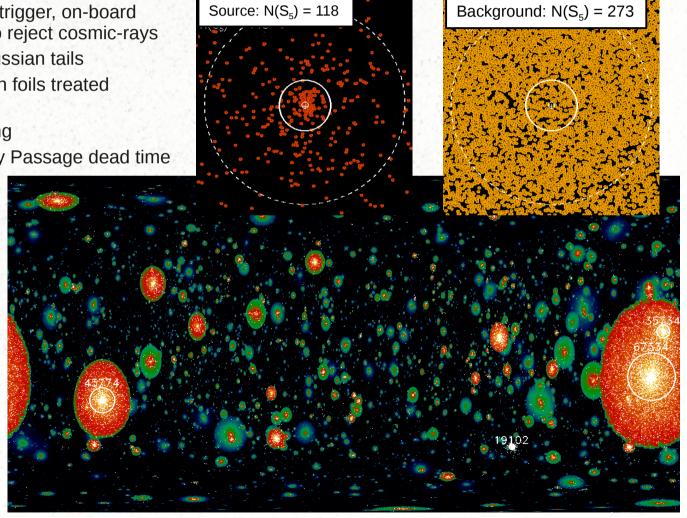
- Selection effects: LAT trigger, on-board filter, offline analysis to reject cosmic-rays
- > PSF includes non-Gaussian tails
- Thin and thick tungsten foils treated separately
- > ±35° instrument rocking
- > South Atlantic Anomaly Passage dead time

Energy-dependent ROI optimization

Calculate detection significance:

$$P = \sum_{i=k}^{\infty} \frac{\lambda^k e^{-\lambda}}{k!}$$

$$S = \sqrt{2} \text{ erf}^{-1} (1 - 2P)$$



Source: $N(S_5) = 118$

Fermi/LAT GTOBSSIM Monte-Carlo Simulation (with Brandon Anderson & Robert Johnson, SCIPP)

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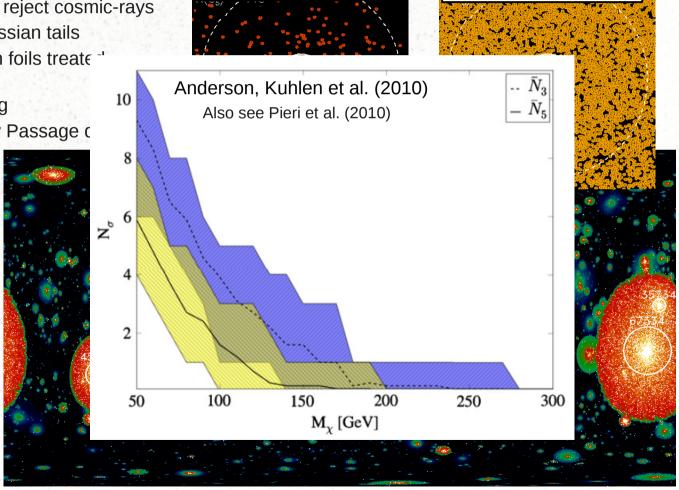
South Atlantic Anomaly Passage c

Energy-dependent ROI optimization

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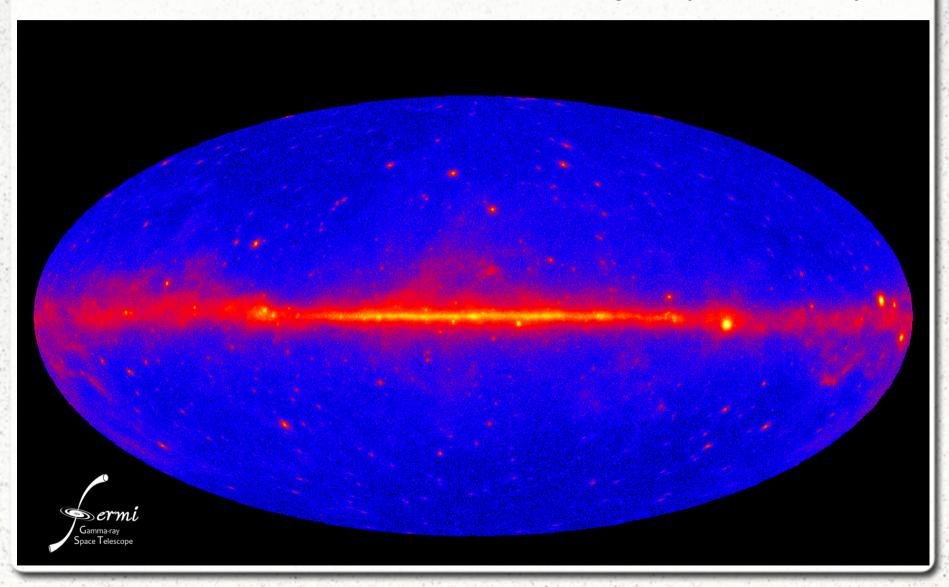
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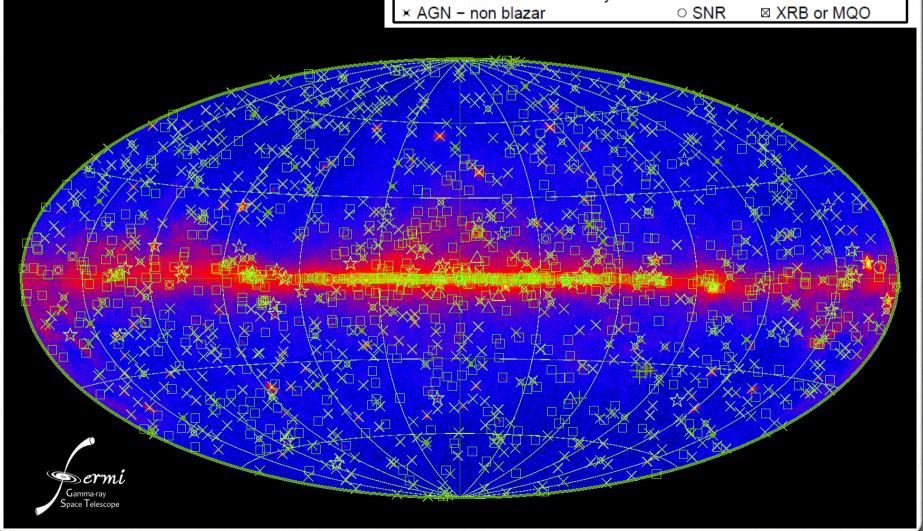
Background: $N(S_5) = 273$

Fermi was launched on June 11th 2008 and has been observing the sky for more than 2 years.



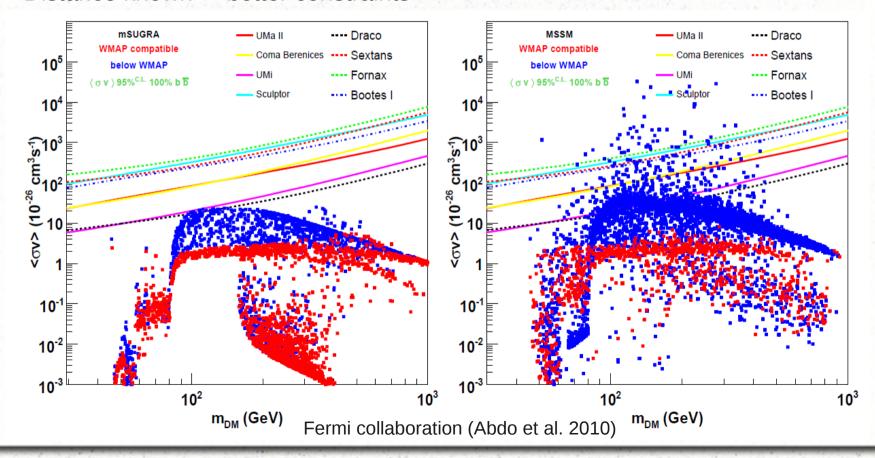
So far, now dark matter signal has been detected. \odot

□ No association □ Possible association with nearby SNR or PWN
× AGN - blazar * Starburst Gal ☆ Pulsar ☆ Pulsar w/PWN
× AGN - unknown + Galaxy ◇ PWN △ Globular cluster
× AGN - non blazar ○ SNR ☑ XRB or MQO



Luminous dwarf satellite galaxies

- Know where to look
- Can stack data
- Targeted observations with ACTs
- Distance known → better constraints



Dark Subhalos

 $E_{\gamma}^2 d\phi/dE_{\gamma} (GeV/s cm^2) G_{\Sigma}$

10

 $E_{\gamma}^2 d\phi/dE_{\gamma} (GeV/s cm^2)$

0.5

Need a large area survey

J2039.4-5621: Annihilation to $b\overline{b}$, $m_{DM} = 71 \text{ GeV}$

E_v (GeV)

E_γ (GeV)

J0707.3+7742: Annihilation to $\tau^+\tau^-$, $m_{DM} = 446 \text{ GeV}$

- Could in principle be very nearby
- Less confusion from astrophysical sources

50 100

50 100

Sources 150

Number of 100

150

50

200

150

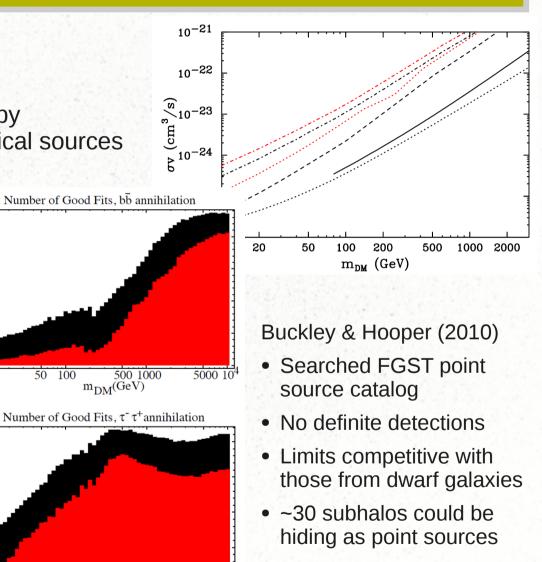
Number of Sources

10

50 100

50 100 500 1000 m_{DM}(GeV)

5000 10

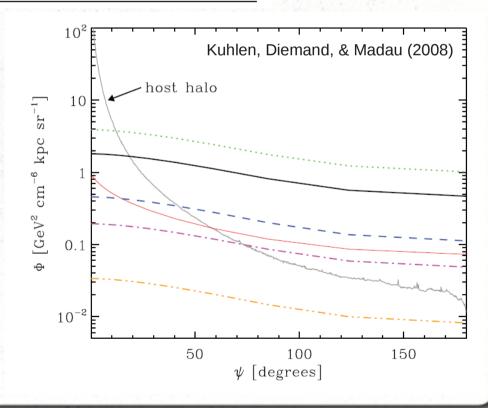


2) Cumulative signal from all Galactic subhalos

| SUBHALO | MASS | FUNCTION | N | ODELS |
|---------|------|----------|---|-------|
| | | | | |

| α | $m_0 \ (M_{\odot})$ | $N_{ m tot}$ | $M_{ m tot} \ (M_{\odot})$ | $f_{ m tot}$ | M_u (M_{\odot}) | f_u |
|-----|---------------------|----------------------|----------------------------|--------------|----------------------|-------|
| 2.0 | 10^{-6} | 2.5×10^{16} | 9.3×10^{11} | 0.53 | 7.0×10^{11} | 0.40 |
| 1.9 | 10^{-6} | 9.2×10^{14} | 3.2×10^{11} | 0.19 | 1.2×10^{11} | 0.070 |
| 1.8 | 10^{-6} | 3.3×10^{13} | 2.1×10^{11} | 0.12 | 3.3×10^{10} | 0.018 |
| 2.0 | 1 | 2.5×10^{10} | 5.8×10^{11} | 0.33 | 3.5×10^{11} | 0.20 |
| 2.0 | 10^{-12} | 2.5×10^{22} | 1.3×10^{12} | 0.73 | 1.0×10^{12} | 0.60 |

- CDM predicts an enormous number of low mass subhalos.
- Their cumulative annihilation signal should result in a diffuse flux.
- Less centrally concentrated than the host halo flux.
- Reduced contrast between center and anti-center. Bad news for IceCube? (Rott et al. 2010)
- Angular fluctuations are an interesting signal to be searched for (Siegal-Gaskins et al. 2008, Ando 2009)



The term "Boost Factor" has been used (abused?) in many ways:

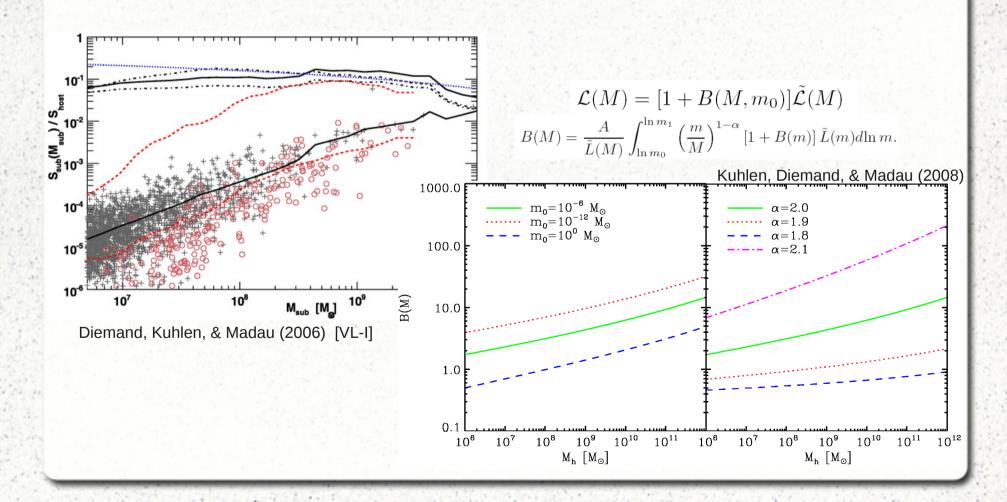
- Enhancement in total halo luminosity from NFW profile compared to a spherical tophat.
- > Enhancement in total halo luminosity from substructure (and subsubstructure, etc.) compared to a smooth NFW density profile.
- > Enhancement of local (8kpc) annihilation rate over (0.3 GeV cm⁻³)².
- > Enhancement of Galactic Center annihilation rate.
- > Enhancement of the surface brightness of angularly resolved subhalos.

There is no one single "Boost Factor"!

The enhancement due to clumpy substructure depends on source location and/or its angular extent.

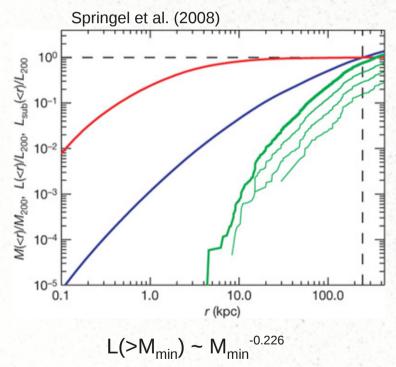
Total Halo Luminosity Boost Factor

- Only applicable to unresolved sources!
- Important for the extragalactic gamma-ray background

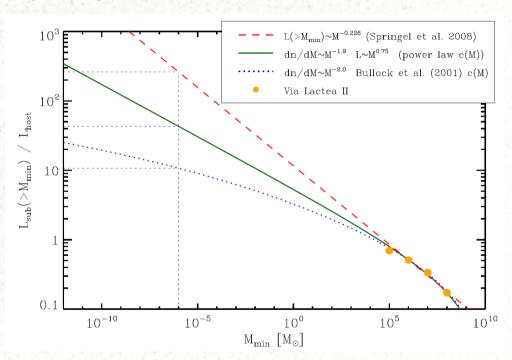


Total Halo Luminosity Boost Factor

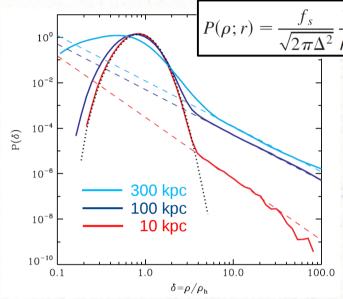
- Only applicable to unresolved sources!
- Important for the extragalactic gamma-ray background.



Total boost factor for $M_{min}=10^{-6} M_{\odot}=232!$

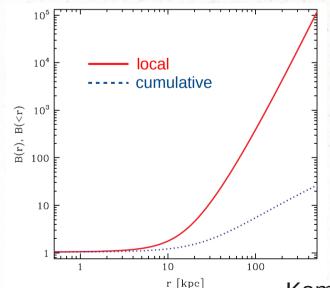


Depends **critically** on what one assumes for the concentration-mass relation for subhalos below the simulations' resolution limit!



- $P(\rho;r) = \frac{f_s}{\sqrt{2\pi\Delta^2}} \frac{1}{\rho} \exp\left\{-\frac{1}{2\Delta^2} \left[\ln\left(\frac{\rho}{\rho_h}e^{\Delta^2/2}\right)\right]^2\right\} + (1 f_s) \frac{1 + \alpha(r)}{\rho_h} \Theta(\rho \rho_h) \left(\frac{\rho}{\rho_h}\right)^{-(2+\alpha)}\right\}$
 - > We measure the PDF of $\rho l \rho_{\rm host}$ in the simulation.
 - It's fit well by a log-normal plus a powerlaw tail due to substructure.

$$\alpha \approx 0.0 \pm 0.1$$
 $1 - f_s(r) = 7 \times 10^{-3} \left(\frac{\bar{\rho}(r)}{\bar{\rho}(r = 100 \text{ kpc})} \right)^{-0.26}$

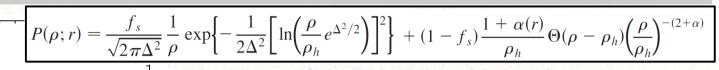


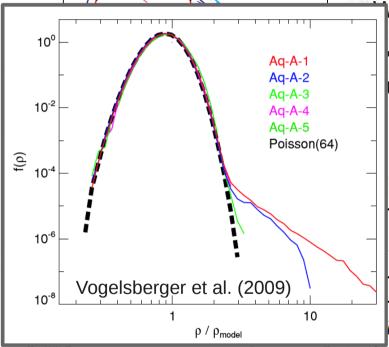
$$B(r) = \frac{\int \rho^2 dV}{\int [\bar{\rho}(r)]^2 dV} = \int_0^{\rho_{\text{max}}} P(\rho, r) \frac{\rho^2}{[\bar{\rho}(r)]^2} d\rho$$

$$B(r) = f_s e^{\Delta^2} + (1 - f_s) \frac{1 + \alpha}{1 - \alpha} \left[\left(\frac{\rho_{\text{max}}}{\rho_h} \right)^{1 - \alpha} - 1 \right]$$

Local boost (e.g. at 8 kpc or at the G.C.) ≠ Total boost

Kamionkowski, Koushiappas & Kuhlen (2010)





10 r [kpc] 100

10°

10-2

10

Ve measure the PDF of ρ/ρ_{host} in the simulation.

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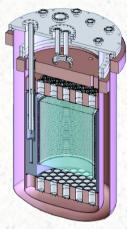
Kamionkowski, Koushiappas & Kuhlen (2010)

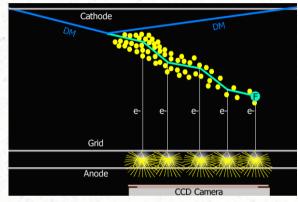
Cryogenic phonon detection (e.g. CDMS)

Liquid Xenon scintillation detectors (e.g. Xenon100, LUX)

Directionally sensitive (e.g. DRIFT, DMTPC)





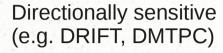


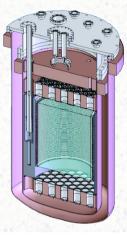
$$\frac{dR}{dE_R} = N_T M_N \frac{\rho_{\chi} \sigma_n}{2m_{\chi} \mu_{ne}^2} \frac{(f_p Z + f_n (A - Z))^2}{f_n^2} F^2[E_R] \int_{\beta_{min}}^{\infty} \frac{f(v)}{v} dv$$

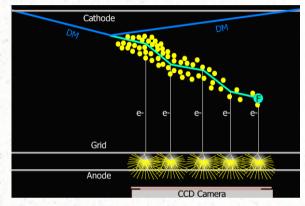
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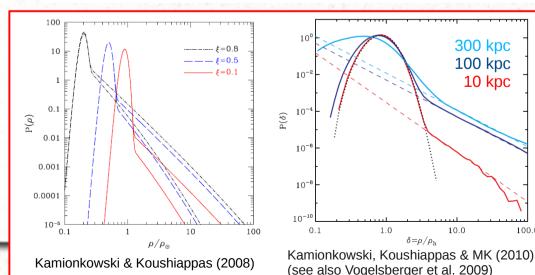
Liquid Xenon scintillation detectors (e.g. Xenon100, LUX)







$$\frac{dR}{dE_R} = N_T M_N \frac{\rho_{\chi} \sigma_n}{2m_{\chi} \mu_{ne}^2} \frac{(f_p Z + f_n (A - Z))^2}{f_n^2} F^2[E_R] \int_{\beta_{min}}^{\infty} \frac{f(v)}{v} dv$$

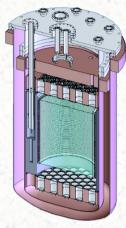


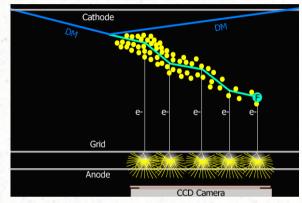
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Directionally sensitive (e.g. DRIFT, DMTPC)

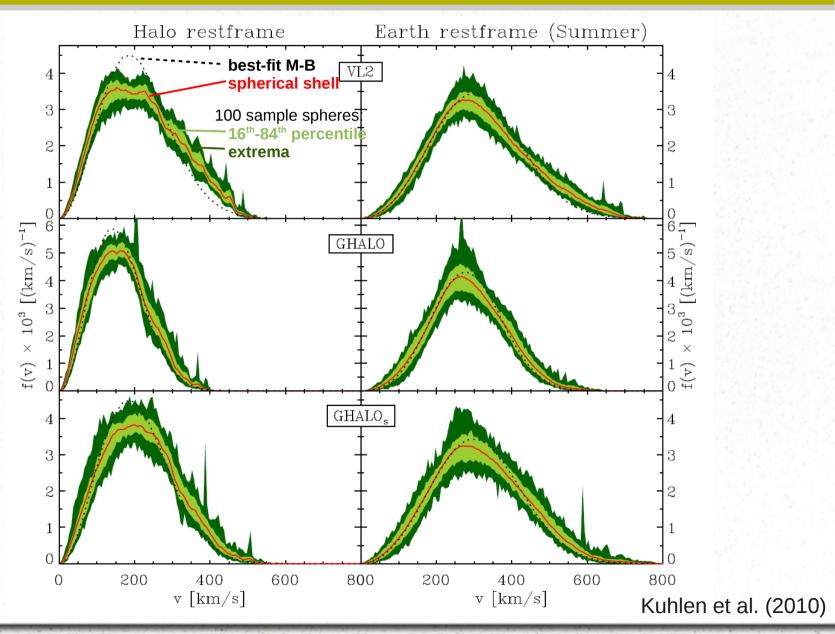






$$\frac{dR}{dE_R} = N_T M_N \frac{\rho_{\chi} \sigma_n}{2m_{\chi} \mu_{ne}^2} \frac{(f_p Z + f_n (A - Z))^2}{f_n^2} F^2[E_R] \int_{\beta_{min}}^{\infty} \frac{f(v)}{v} dv$$

Velocity Space Substructure



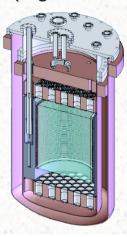
See also: Hansen et al. (2005), Vogelsberger et al. (2009)

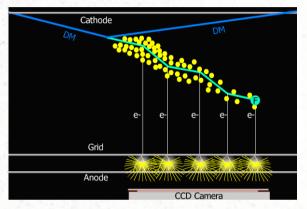
Cryogenic phonon detection (e.g. CDMS)

Cig. CDIVIO)

Liquid Xenon scintillation detectors (e.g. Xenon100, LUX)

Directionally sensitive (e.g. DRIFT, DMTPC)





$$\frac{dR}{dE_R} = N_T M_N \frac{\rho_{\chi} \sigma_n}{2m_{\chi} \mu_{ne}^2} \frac{(f_p Z + f_n (A - Z))^2}{f_n^2} F^2[E_R] \int_{\beta_{min}}^{\infty} \frac{f(v)}{v} dv$$

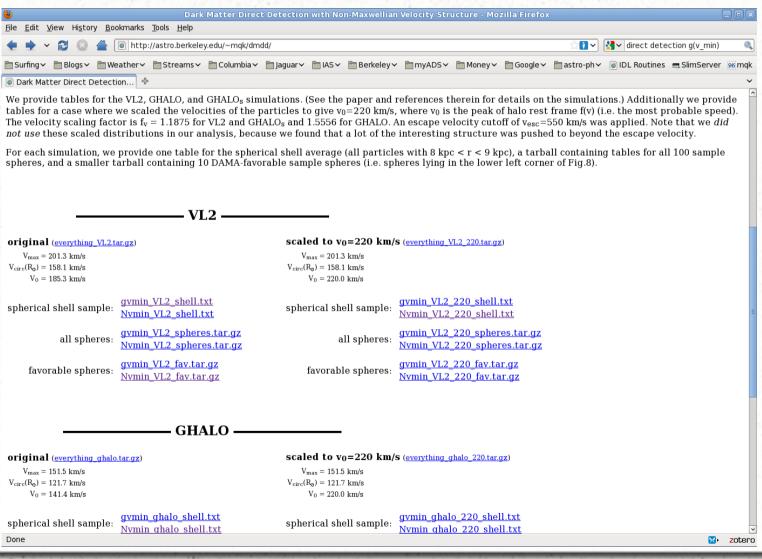
$$\beta_{\min} = \sqrt{\frac{1}{2m_N E_R}} \left(\frac{m_N E_R}{\mu} + \delta \right)$$

f(v) is not Maxwellian!

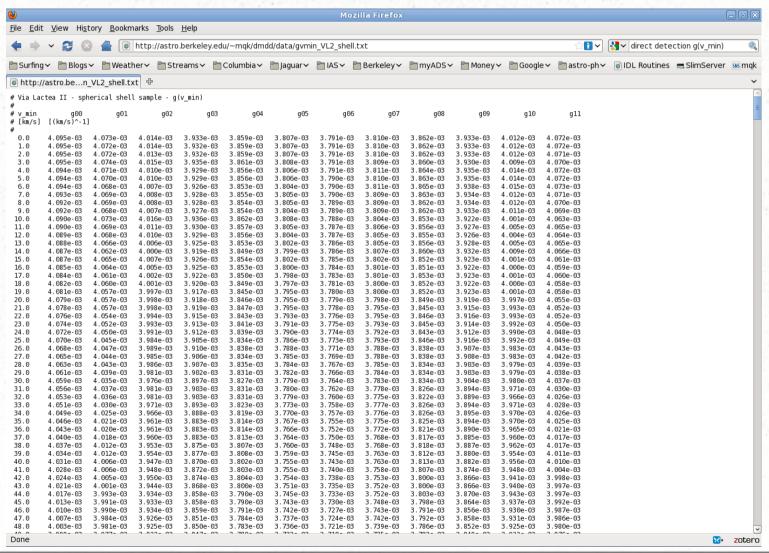
Substructures can be important if β_{\min} is large.

- > Inelastic DM (δ >0)
- Light DM (M_x<10GeV)</p>
- \succ Directionally sensitive experiments often require high E_{recoil} , large β_{min} .

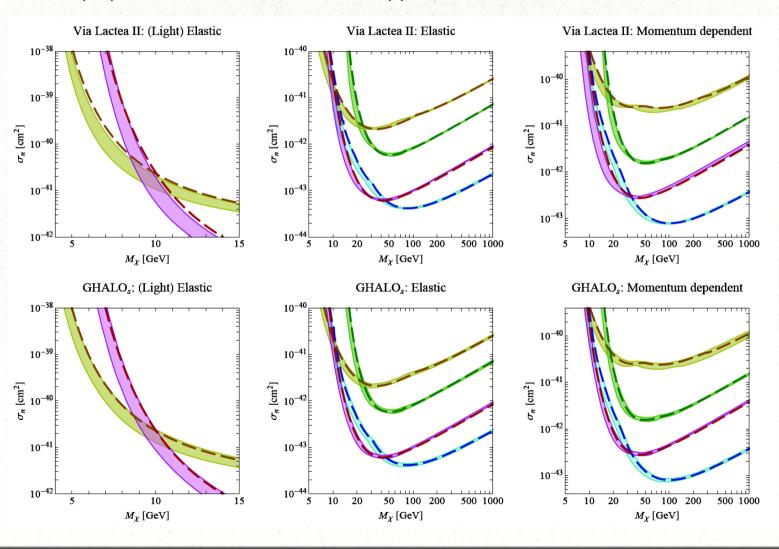
Tables of
$$g(v_{\min}) = \int_{v_{\min}}^{\infty} \frac{f(v)}{v} \; dv$$
 are available for download, at:



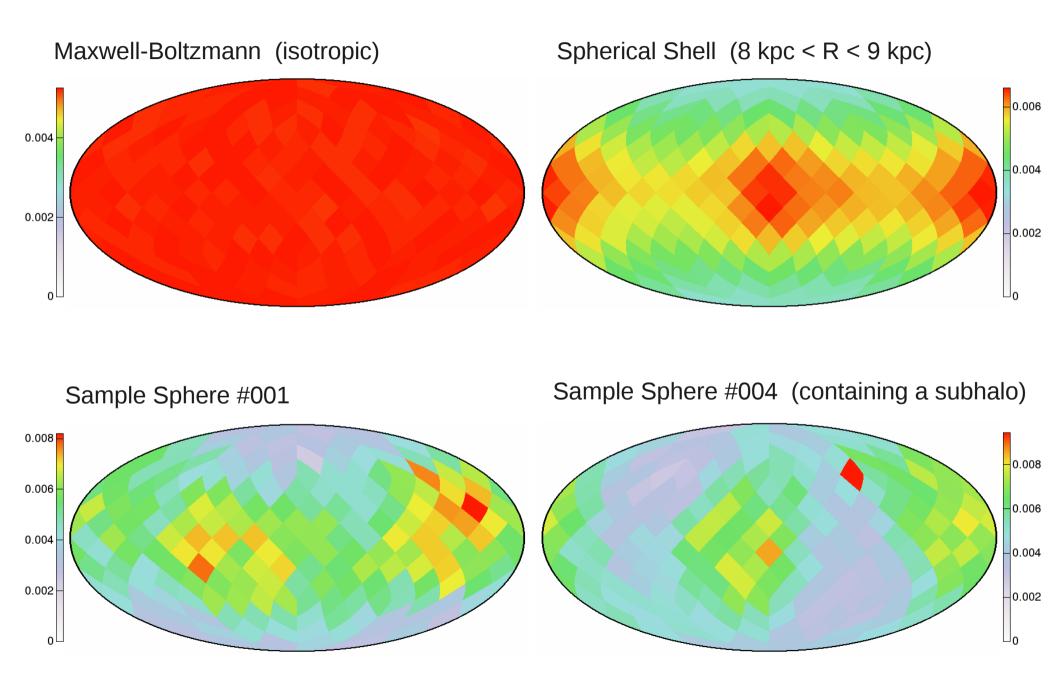
Tables of
$$g(v_{\min}) = \int_{v_{\min}}^{\infty} \frac{f(v)}{v} \ dv$$
 are available for download, at:



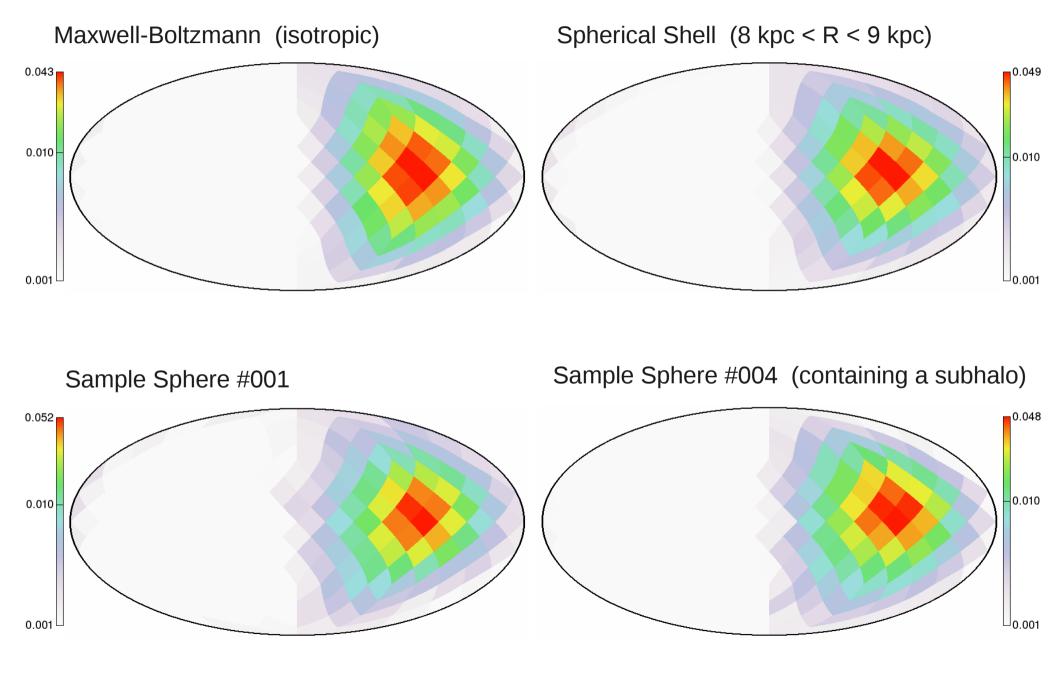
McCabe (2010) made use of these tables to evaluate the dependence of exclusion limits from CDMS-II(Si), CDMS-II(Ge), CRESST-II, XENON10 on the f(v) variation from the VL2/GHALO simulations.



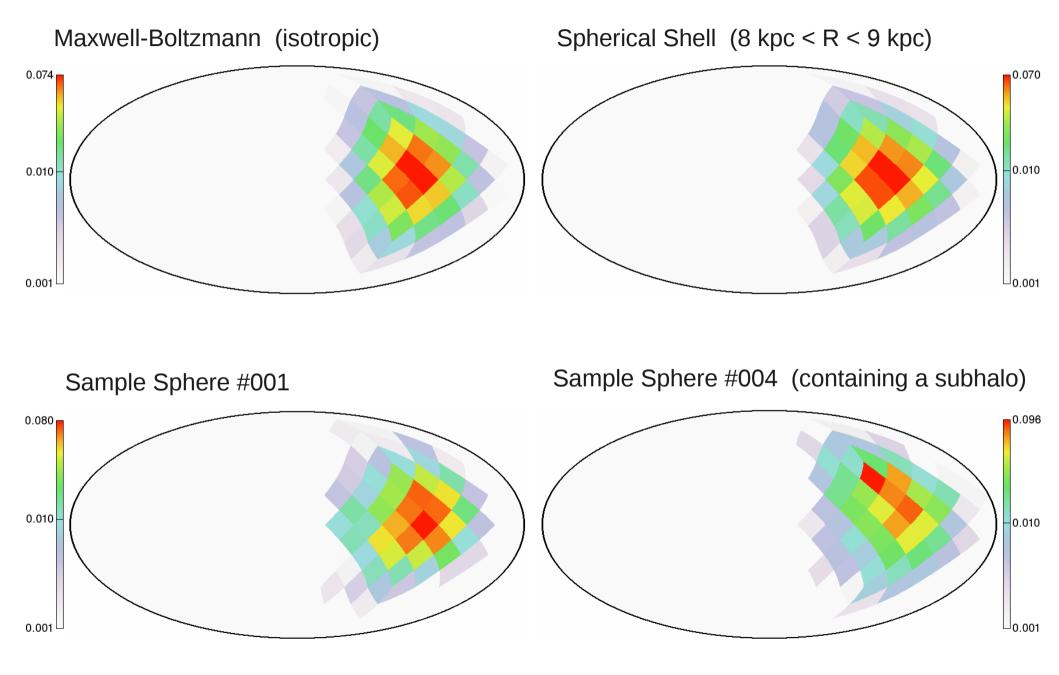
Velocity Direction in Halo Rest Frame



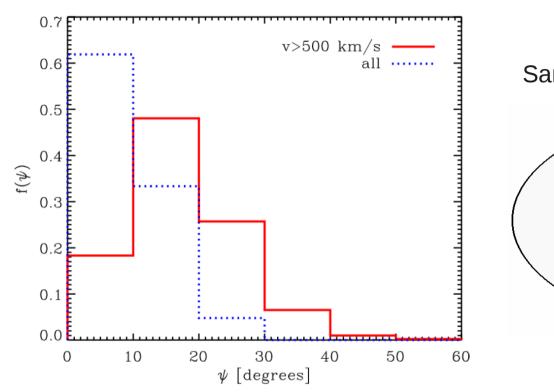
... in Earth Rest Frame v_{min}= 0 km/s

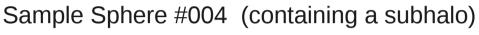


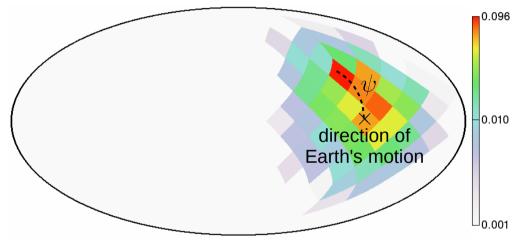
... in Earth Rest Frame v_{min} = 500 km/s



... in Earth Rest Frame v_{min} = 500 km/s







At v_{min} =500 km/s the hotspot is more than 10° away from the direction of Earth's motion in ~80% of all cases!

Conclusions

- The number of subhalos resolved in the to-date largest simulations (Via Lactea II, GHALO, Aquarius) is ever increasing: >300,000 at latest count. Also lots of velocity substructure from subhalos and tidal streams.
- Once properly scaled, the Via Lactea, GHALO, and Aquarius simulations give consistent results.
- Simulations predict that Fermi should discover a handful of subhalos over its lifetime if the DM mass is <100 GeV and it annihilates through bb. So far only limits.
- > The annihilation boost factor from substructure depends on radius: at the GC or at the Sun it's not likely to be important.
- > The total luminosity boost factor critically depends on the extrapolation of the subhalo concentration-mass relation.
- Velocity substructure in the DM distribution function might noticeably affect DM direct detection experiments, especially for DM models or experimental setups that are sensitive to high velocity DM particles: e.g. inelastic DM, light DM, directionally sensitive experiments.